AQA

A-LEVEL
Mathematics

Pure Core 1 – MPC1
Mark scheme

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Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
√or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
–*x* EE	deduct *x* marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

Q	Solution	Mark	Total	Comment
1				
(a)(i)	Grad $AB = \dfrac{-5-2}{3--1}$ OE	**M1**		correct unsimplified eg $\dfrac{2--5}{-1-3}$
	$= -\dfrac{7}{4}$	**A1**	**2**	
(ii)	$y--5 = \text{'their grad'}\ (x-3)$ $y-2 = \text{'their grad'}\ (x--1)$	**M1**		either pair of coordinates used correctly and attempt to find c if using $y=mx+c$
	$y-2=-\dfrac{7}{4}(x+1)$ $y+5=-\dfrac{7}{4}(x-3)$ $y=-\dfrac{7}{4}x+\dfrac{1}{4}$	**A1**		OE, any form of correct equation with – – simplified to +
	$7x+4y=1$	**A1**	**3**	integer coefficients & in this form
(b)(i)	$(M)\quad (1,-1.5)$	**B1**	**1**	condone $x=1,\ y=-\dfrac{3}{2}$
(ii)	Perp grad = $\dfrac{4}{7}$	**B1√**		perp grad = –1/ 'their' grad AB
	$y--\dfrac{3}{2} = \text{'their'}\dfrac{4}{7}(x-1)$	**M1**		ft 'their M' but must have attempted perpendicular gradient
	$y+\dfrac{3}{2}=\dfrac{4}{7}(x-1)$	**A1**	**3**	**any** correct form with – – simplified to + eg $8x-14y=29$; $y=\dfrac{4}{7}x+c, c=-\dfrac{29}{14}$
(c)	$(AC^2=)\quad (k--1)^2+(2k+3-2)^2$	**M1**		$(k+1)^2+(2k+1)^2$
	$k^2+2k+1+4k^2+4k+1=13$ $5k^2+6k-11=0$	**A1**		
	$(5k+11)(k-1)=0$	**A1**		correct factors or correct use of formula as far as $\dfrac{-6\pm\sqrt{256}}{10}$
	$\Rightarrow k=1,\quad k=-\dfrac{11}{5}$	**A1**	**4**	
	Total		**13**	

(a) (i) **NMS** grad $AB = -\dfrac{7}{4}$ earns 2 marks.

(ii) must simplify $y--5$ to $y+5$ or $x--1$ to $x+1$ for first **A1**

Condone $8y+14x=2$ etc for final **A1**, but not $7x+4y-1=0$ etc

(b)(ii) If their gradient of AB is m, then use of $-m$ or $1/m$ can earn **M1** . For **A1**, $1/\left(\frac{7}{4}\right)$, $\frac{14.5}{7}$ etc must be simplified.

Q	Solution	Mark	Total	Comment
2	$\dfrac{15+7\sqrt{3}}{9+5\sqrt{3}}\times\dfrac{9-5\sqrt{3}}{9-5\sqrt{3}}$	**M1**		writing correct quotient and multiplying by correct conjugate of denominator
	(Numerator =) $135-75\sqrt{3}+63\sqrt{3}-105$	**A1**		$30-12\sqrt{3}$
	(Denominator = $81-45\sqrt{3}+45\sqrt{3}-75$) $= 6$	**B1**		must be seen as denominator
	$\left(\dfrac{30-12\sqrt{3}}{6}=\right)\quad 5-2\sqrt{3}$	**A1cso**	**4**	units (cm) need not be given
	Alternative			
	$(9+5\sqrt{3})(m+n\sqrt{3})$			
	$=9m+15n+5m\sqrt{3}+9n\sqrt{3}$	**(M1)**		must be correct
	$9m+15n=15,\quad 5m+9n=7$	**(A1)**		both equations correct
	$m=5\quad,\quad n=-2$	**(A1)**		either correct
	$5-2\sqrt{3}$	**(A1)**		
	Total		**4**	

No marks if candidate uses $\dfrac{9+5\sqrt{3}}{15+7\sqrt{3}}$

Condone multiplication by $9-5\sqrt{3}$ instead of $\dfrac{9-5\sqrt{3}}{9-5\sqrt{3}}$ for **M1 only if** subsequent working shows multiplication by **both** numerator and denominator – otherwise **M0**.

May use alternative conjugate $\dfrac{15+7\sqrt{3}}{9+5\sqrt{3}}\times\dfrac{5\sqrt{3}-9}{5\sqrt{3}-9}$ **M1** numerator $=12\sqrt{3}-30$ **A1** denominator = –6 **B1**

Ignore any incorrect units

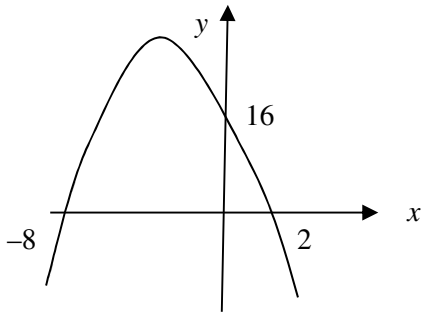
Q	Solution	Mark	Total	Comment
3 (a)(i)	$\left(\frac{dy}{dx}=\right)\ 10x^4+20x^3$	**M1**		one term correct
		A1	**2**	all correct (no + c etc)
(ii)	$\left(\frac{d^2y}{dx^2}=\right)\ 40x^3+60x^2$	**B1√**	**1**	ft their $\frac{dy}{dx}$
(b)(i)	$\left(\frac{dy}{dx}=\right)\ 10-20\ \ =-10$	**B1√**		correctly sub $x=-1$ into their $\frac{dy}{dx}$ and evaluated correctly
	$\frac{dy}{dx}<0$ (therefore y is) decreasing	**E1√**	**2**	Must state "decreasing" **and** $\frac{dy}{dx}<0$ ft 'therefore y is increasing' **and** reason if their value of $\frac{dy}{dx}>0$
(ii)	(When $x=-1$) $y=2$	**B1**		
	$y-'their'2='their\ grad'(x--1)$ but must be tangent and not normal	**M1**		ft ' their' value of $\frac{dy}{dx}$ when $x=-1$ and ' their' y-coordinate
	$y-2=-10(x+1)$ *or* $y=-10x-8$ etc	**A1**	**3**	any correct tangent eqn from correct $\frac{dy}{dx}$
(c)	$\left(\frac{dy}{dx}=\right)\ 10(-2)^4+20(-2)^3$	**M1**		correctly sub $x=-2$ into their $\frac{dy}{dx}$
	$=160-160=0\ \Rightarrow$ **stationary** point (when $x=-2$)	**A1**		correctly shown that $\frac{dy}{dx}=0$ **plus** correct statement
	$\left(\frac{d^2y}{dx^2}=\right)\ 40(-2)^3+60(-2)^2$	**M1**		correctly sub $x=-2$ into their $\frac{d^2y}{dx^2}$ or other suitable test for max/min
	$=-320+240=-80<0$ (Therefore) **maximum** (point at Q)			**either** $\frac{d^2y}{dx^2}=-320+240<0$
		A1	**4**	**or** $\frac{d^2y}{dx^2}=-80<0$ **plus** conclusion
	Total		**12**	

(b) (i) Accept "gradient is negative so decreasing" for **E1**

Do **not** accept "because **it** is negative" or "$\frac{dy}{dx}=-10$" as reasons for **E1**

(ii) May earn **M1** for attempt to find c using $y=mx+c$ if clearly finding tangent and not normal.
Must simplify $x--1$ to $x+1$ for **A1**

(c) May write "their" $10x^4+20x^3=0$ and attempt to find x for first **M1**
leading to "$x=-2$ …stationary pt" for **A1**

Q	Solution	Mark	Total	Comment
4				
(a)(i)	$k-(x+3)^2$	**M1**		*or* $x^2+6x-16=(x+3)^2-25$ *or* $q = 3$ stated
	$25-(x+3)^2$	**A1**	**2**	
(ii)	(Max value =) 25	**B1**√	**1**	ft their p
(b)(i)	$(8+x)(2-x)$	**B1**	**1**	
(ii)		**M1**		∩ shape
		A1		curve roughly symmetrical with max to left of y-axis, curve in all 4 quadrants **and** y-intercept 16 stated or marked on y-axis
	crosses x-axis at –8 and 2	**B1**	**3**	correct - stated or marked on x-axis
	Total		**7**	

(a)(i) **Example** $16-(x+3)^2-9$ earns **M1**

(ii) (–3, 25) scores **B0** since maximum value not identified
Allow maximum given as "$y = 25$"

(b)(i) Condone $-(x-2)(x+8)$, $(x-2)(-x-8)$ etc

(ii) Withhold **B1** if more than 2 intercepts

Q	Solution	Mark	Total	Comment
5				
(a)	$(-3)^3 + c(-3)^2 + d(-3) + 3$	**M1**		p(–3) attempted
	$-27 + 9c - 3d + 3 = 0$			must see this line or equivalent, **and** must have = 0 on right or left before final result
	$\Rightarrow 3c - d = 8$	**A1**	**2**	**AG** be convinced
(b)	$2^3 + c \times 2^2 + d \times 2 + 3 = 65$	**M1**		p(2) attempted & … = 65
	$8 + 4c + 2d + 3 = 65$	**A1**	**2**	correct equation in any form simplifying powers of 2 eg $4c + 2d = 54$
(c)	$5c = 35$			correct elimination of c or d using both $3c - d = 8$ and their equation from (b)
	or $10d = 130$ OE	**M1**		
	$c = 7$	**A1**		
	$d = 13$	**A1**	**3**	
	Total		**7**	

(a) May use long division by $x + 3$ but must reach remainder term for **M1**
Condone missing brackets in p(–3) expression if recovered later as –27 +9c +… to earn **A1**

Treat parts **(b)** and **(c)** holistically

(b) May use long division by $x - 2$ as far as remainder and equate their remainder to 65 for **M1**

(c) **Example** $4c + 2(3c - 8) = 54$ earns **M1** for eliminating d if equation in part **(b)** is correct

Q	Solution	Mark	Total	Comment
6				
(a)(i)	$x^3 - x^2 - 5x + 7 = x + 7$	**M1**		
	$\Rightarrow x^3 - x^2 - 5x = x$			must see this line OE eg $x^3 - x^2 - 6x = 0$
	$(x \neq 0) \Rightarrow x^2 - x - 6 = 0$	**A1**	**2**	**AG**
(ii)	$(x-3)(x+2)$	**M1**		correct
	$x = 3, \quad x = -2$	**A1**		both x values correct
	$A(-2,5)$ **and** $C(3,10)$	**A1**	**3**	both pairs of coordinates correct
(b)	$\frac{x^4}{4} - \frac{x^3}{3} - \frac{5x^2}{2} + 7x \quad (+c)$	**M1** **A1** **A1**	**3**	2 terms correct another term correct all correct
(c)	$F(-2) = \left[\frac{(-2)^4}{4} - \frac{(-2)^3}{3} - \frac{5(-2)^2}{2} + 7(-2)\right]$	**M1**		F('their'–2) correctly substituting into their answer to (b) , but must have scored M1 in part (b)
	F(0) – F(–2) = $0 - \left(\frac{16}{4} + \frac{8}{3} - \frac{20}{2} - 14\right) = \frac{52}{3}$	**A1**		correct value using limits correctly
	Area of trapezium = $\left(\frac{1}{2}(5+7)\times 2\right) = 12$	**B1**		or rectangle plus triangle
	Area of $R = \frac{52}{3} - 12 = \frac{16}{3}$	**A1**	**4**	$5\frac{1}{3}$ or $5.\dot{3}$
	Total		**12**	

(a)(ii) **NMS either** $(-2,5)$ **or** $(3,10)$ scores **SC1** and **both correct** scores **SC3**
Allow "when $x = 3, \quad y = 10$ **and** when $x = -2, \quad y = 5$" instead of coordinates for final **A1**

(c) Condone missing brackets around "their" –2 for **M1** and if recovered and correct on next line for **A1**
Area of trapezium found by integration $\int_{-2}^{0} (x+7)\,dx = \left[\frac{x^2}{2} + 7x\right]_{-2}^{0} = 12$ earns **B1**
Accept rounded answer of 5.3 etc after correct exact answer seen.

Q	Solution	Mark	Total	Comment
7				
(a)	$(x-5)^2+(y--6)^2$	**M1**		one term correct
		A1		LHS correct with perhaps extra constant terms
	$(x-5)^2+(y+6)^2=20$	**A1**	**3**	equation completely correct
(b) (i)	$C(5,-6)$	**B1**√	**1**	correct or ft their **(a)**
(ii)	(radius =) $\sqrt{20}$	**M1**		correct or ft 'their' $\sqrt{k}$ provided RHS > 0
	$= 2\sqrt{5}$	**A1**	**2**	must see $\sqrt{20}$ **first**
(c)	Grad $AC = \dfrac{-6--2}{5-3}$ $(=-2)$	**M1**		correct unsimplified, ft their coords of C
	Grad of tangent $= \dfrac{1}{2}$	**B1**√		ft their $-1/$ grad AC
	Equation of tangent is $(y--2)="their\frac{1}{2}"(x-3)$	**M1**		clear attempt at **tangent** not normal through $(3, -2)$
	$y+2=\dfrac{1}{2}(x-3)$	**A1**		correct equation in any form but $y--2$ must be simplified to $y+2$
	$x-2y=7$	**A1 cso**	**5**	
(d)	$AB^2+(their\ \ r)^2 = 6^2$	**M1**		Pythagoras used with 6 as hypotenuse
	$d^2+20=36$ *or* $(AB^2)=36-20$	**A1**		values correct with $(2\sqrt{5})^2=20$ PI
	$AB^2=16$ Hence $AB=4$	**A1cso**	**3**	notation all correct
	Total		**14**	

(a) $(x-5)^2+(y--6)^2=\left(\sqrt{20}\right)^2$ scores full marks

If final equation is correct then award 3 marks, treating earlier lines with extra terms etc as rough working.
If final equation has sign errors then check to see if M1 is earned.
Example $(x-5)^2+(y+6)^2-25+36+41=0$ earns **M1 A1** but if this is part of preliminary working and final equation is offered as $(x-5)^2+(y+6)^2=20$ then award **M1 A1 A1.**
Example $(x-5)^2+(y-6)^2=20$ earns **M1 A0 ; Example** $(x+5)^2+(y-6)^2=20$ earns **M0**

(b)(ii) Candidates may still earn A1 here provided RHS of circle equation is 20.
Example $(x+5)^2+(y-6)^2=20$ earns **M0** in **(a)** but can then earn **M1 A1** for radius = $\sqrt{20}=2\sqrt{5}$
NMS or no $\sqrt{20}$ seen; " radius $=2\sqrt{5}$ **"** scores **SC1** since question says "show that"

(c) May earn second **M1** for attempt to find c using $y=mx+c$ if clearly finding tangent and not normal.
If their gradient of AC is m, then use of $-m$ or $1/m$ with correct coordinates can earn second **M1**

(d) **Example** $AB=36-(2\sqrt{5})^2=16=4$ scores **M1 A1 A0** for poor notation
NMS $AB=4$ scores **SC1** since no evidence that exact value of radius has been used.

Q	Solution	Mark	Total	Comment
8				
(a)	$3-6x-15x-10>0$	**M1**		Correctly multiplied out with >0
	$-21x>7$			
	$\Rightarrow x<-\frac{1}{3}$	**A1cso**	**2**	all working correct
(b)	$6x^2-x-12\leqslant 0$			
	$(3x+4)(2x-3)$	**M1**		correct factors or correct use of formula as far as $\frac{1\pm\sqrt{289}}{12}$
	CVs are $-\frac{4}{3}$, $\frac{3}{2}$	**A1**		
	+ - + at $-\frac{4}{3}$ and $\frac{3}{2}$	**M1**		use of sign diagram or graph with CVs clearly shown
	$-\frac{4}{3}\leqslant x\leqslant\frac{3}{2}$	**A1**	**4**	*or* $\frac{3}{2}\geqslant x\geqslant-\frac{4}{3}$
	Total		**6**	
	TOTAL		**75**	

(a) Allow final answer in form $-\frac{1}{3}>x$ **.**

(b) For second **M1**, if critical values are correct then sign diagram or sketch $\vee$ must be correct ***with correct CVs marked***.
However, if CVs are not correct then second **M1** can be earned for attempt at sketch or sign diagram but ***their CVs*** MUST be marked on the diagram or sketch.
Final **A1,** inequality must have x and no other letter.

Final answer of $x\leqslant\frac{3}{2}$ AND $x\geqslant-\frac{4}{3}$ (with or without working) scores 4 marks .

(A) $-\frac{4}{3}<x<\frac{3}{2}$ (B) $x\leqslant\frac{3}{2}$ OR $x\geqslant-\frac{4}{3}$ (C) $x\leqslant\frac{3}{2}$, $x\geqslant-\frac{4}{3}$ **(D)** $-\frac{4}{3}\leqslant k\leqslant\frac{3}{2}$
with or without working each score 3 marks **(SC3)**

Example NMS $\frac{4}{3}\leqslant x\leqslant\frac{3}{2}$ scores **M0** (since one CV is incorrect)

Example NMS $x<\frac{3}{2}$, $x<-\frac{4}{3}$ scores **M1 A1 M0** (since both CVs are correct)